# Dice and Coin Simulations 

## using random numbers on a spreadsheet

The aims of this session are to enable you to use a spreadsheet to

- simulate throwing dice and tossing coins,
- record your results in a table,
- illustrate your results graphically,
- make comparisons between observed and expected frequencies.


## Random Numbers

Random numbers are generated using the function =RAND() as follows:

| Random number | Format | Example |
| :--- | :--- | :--- |
| Decimal in range 0 to 1 | =RAND() | 0.2341232786 |
| Decimal in range 0 to 6 | $=6^{* R A N D() ~}$ | 1.404739672 |
| Integer 0, 1, 2, 3, 4 or 5 | =INT(6*RAND()) | 1 |
| Integer 1, 2, 3, 4, 5 or 6 | $=$ =INT(6*RAND())+1 | 2 |
| Integer 0 or 1 | =INT(2*RAND()) | 0 |

## Simulating dice throwing (1): Single die

- Design a spreadsheet to simulate the throwing of a die 100 times.
- Record your results as indicated below.
- Use the function =COUNTIF(Start cell : Finish cell , $x$-cell) to record the frequency of each $x$-value.
- Use the "chart wizard" to produce a bar chart to illustrate the frequency distribution.

| Dice score |  |
| ---: | ---: |
| 1 | 6 |
| 2 | 5 |
| 3 | 2 |
| 4 | 2 |
| 5 | 6 |
| 6 | 6 |
| 7 | 1 |
| 8 | 6 |
| 9 | 1 |
| 10 | 5 |
| 11 | 5 |
| 12 | 3 |
| 13 | 5 |
| 14 | 3 |
| 15 | 4 |
| 16 | 1 |
| 17 | 3 |
| 18 | 2 |
| 19 | 5 |
| 20 | 3 |
| etc. | etc. |


| $x$ | $f$ |
| ---: | ---: |
| 1 | 21 |
| 2 | 15 |
| 3 | 19 |
| 4 | 12 |
| 5 | 20 |
| 6 | 13 |
| Total | 100 |



## Simulating dice throwing (2): Sum of two dice

Make a copy of the first spreadsheet and modify it to do the following:

- Design a spreadsheet to simulate the throwing of two dice 100 times.
- Record your results in two columns.
- Add a column to represent the total of the two scores.
- Use the function =COUNTIF(Start cell : Finish cell , $x$-cell) to record the frequency of each $x$-value, where $x$ represents the total score.
- Use the "chart wizard" to produce a bar chart to illustrate the frequency distribution.
- Repeat the simulation many times by pressing F9.
- Which is the most popular total? Is it always the same? Should it be the same "in the long run"?
- Extend the simulation to 1000 pairs of values.
- Are there any differences between the pattern for 100 pairs of throws and 1000 pairs of throws?
- Complete the following table for the possible 36 possible totals when two dice are thrown:

| + | 1 | 2 | 3 | 4 | 5 | 6 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 |  |  |  |  |  |  |
| 2 |  |  |  |  |  |  |
| 3 |  |  |  |  |  |  |
| 4 |  |  |  |  |  |  |
| 5 |  |  |  |  |  |  |
| 6 |  |  |  |  |  |  |

- Use the table to generate a column of expected frequencies for your simulation.
- Plot both "observed frequencies" and "expected frequencies" on your chart.
- Are your "observed frequencies" similar to the "expected frequencies"?


## Simulating dice throwing (3): Absolute difference of two dice

Make a copy of the second spreadsheet and modify it to do the following:

- Change the "total" column to an "absolute difference" column.
- Use the function $=$ COUNTIF(Start cell : Finish cell , $x$-cell) to record the frequency of each $x$-value, where $x$ represents the absolute difference between the scores.
- Use the "chart wizard" to produce a bar chart to illustrate the frequency distribution.
- Repeat the simulation many times by pressing F9.
- Which is the most popular difference? Is it always the same? Should it be the same "in the long run"?
- Extend the simulation to 1000 pairs of values.
- Are there any differences between the pattern for 100 pairs of throws and 1000 pairs of throws?


## Pascal's Triangle

Design a spreadsheet to produce Pascal's Triangle, filling in automatically the empty boxes:

|  | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | Total |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0 | 1 |  |  |  |  |  |  |  |  |  |  | 1 |
| 1 | 1 | 1 |  |  |  |  |  |  |  |  |  | 2 |
| 2 | 1 | 2 | 1 |  |  |  |  |  |  |  |  | 4 |
| 3 | 1 | 3 | 3 | 1 |  |  |  |  |  |  |  | 8 |
| 4 | 1 |  |  |  |  |  |  |  |  |  |  |  |
| 5 | 1 |  |  |  |  | 1 |  |  |  |  |  |  |
| 6 | 1 |  |  |  |  |  | 1 |  |  |  |  |  |
| 7 | 1 |  |  |  |  |  |  | 1 |  |  |  |  |
| 8 | 1 |  |  |  |  |  |  |  | 1 |  |  |  |
| 9 | 1 |  |  |  |  |  |  |  |  | 1 |  |  |
| 10 | 1 |  |  |  |  |  |  |  |  |  | 1 |  |

## Simulating coin tossing (1): Number of heads from tossing 4 coins

Make a copy of the second spreadsheet and modify it to do the following:

- Design a spreadsheet to simulate the throwing of four coins 100 times, representing a 'tail' by 0 and a 'head' by 1 .
- Record your results in four columns.
- Add a column to represent the total of the four scores.
- Use the function $=$ COUNTIF(Start cell : Finish cell , $x$-cell) to record the frequency of each $x$-value, where $x$ represents the number of heads.
- Use the "chart wizard" to produce a bar chart to illustrate the frequency distribution.
- Repeat the simulation many times by pressing F9.
- Which is the most popular number of heads? Is it always the same? Should it be the same "in the long run"?
- Extend the simulation to 1000 groups of tossing 4 coins.
- Are there any differences between the pattern for 100 groups and 1000 groups?
- Use a row of Pascal's Triangle to generate a column of expected frequencies for your simulation.
- Plot both "observed frequencies" and "expected frequencies" on your chart.
- Are your "observed frequencies" similar to the "expected frequencies"?


## Simulating coin tossing (2): Number of heads from tossing 5 coins

Make a copy of the last spreadsheet and modify it to simulate the tossing of 5 coins, rather than 4 coins.

- What changes will you have to make to your previous spreadsheet?
- What differences are there in the expected outcomes for each number of heads?

COIN SIMULATION : Tossing 5 coins : Observed and Expected Frequencies

|  | coin | 2nd Coin | 3rd coin | 4th coin | 5th coin | Total | X | f observed | f expected |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 0 | 0 | 0 | 1 | 0 | 1 | 0 | 0 | 3.125 |
| 2 | 1 | 1 | 1 | 1 | 0 | 4 | 1 | 20 | 15.625 |
| 3 | 0 | 0 | 0 | 1 | 1 | 2 | 2 | 30 | 31.25 |
| 4 | 0 | 1 | 1 | 1 | 1 | 4 | 3 | 37 | 31.25 |
| 5 | 0 | 1 | 1 | 0 | 0 | 2 | 4 | 13 | 15.625 |
| 6 | 1 | 1 | 0 | 1 | 0 | 3 | 5 | 0 | 3.125 |
| 7 | 1 | 0 | 1 | 1 | 1 | 4 | Total | 100 |  |
| 8 | 1 | 0 | 1 | 0 | 1 | 3 |  |  |  |
| 9 | 1 | 1 | 0 | 1 | 0 | 3 |  |  |  |
| 10 | 1 | 1 | 0 | 1 | 1 | 4 |  |  |  |
| 11 | 0 | 0 | 0 | 1 | 0 | 1 |  |  |  |
| 12 | 0 | 0 | 1 | 1 | 0 | 2 |  |  |  |
| 13 | 1 | 1 | 0 | 1 | 1 | 4 |  |  |  |
| 14 | 0 | 0 | 1 | 1 | 1 | 3 |  |  |  |
| 15 | 1 | 1 | 0 | 1 | 0 | 3 |  |  |  |
| 16 | 1 | 0 | 1 | 1 | 1 | 4 |  |  |  |
| 17 | 1 | 0 | 0 | 0 | 1 | 2 |  |  |  |
| 18 | 0 | 0 | 0 | 1 | 1 | 2 |  |  |  |
| 19 | 1 | 0 | 0 | 1 | 0 | 2 |  |  |  |
| 20 | 0 | 0 | 0 | 1 | 0 | 1 |  |  |  |
| 21 | 0 | 1 | 1 | 0 | 1 | 3 |  |  |  |
| 22 | 1 | 1 | 1 | 1 | 0 | 4 |  |  |  |
| 23 | 0 | 0 | 1 | 1 | 0 | 2 |  |  |  |
| 24 | 0 | 1 | 1 | 1 | 1 | 4 |  |  |  |
| etc. | etc. | etc. | etc. | etc. | etc. | etc. |  |  |  |



